

Instructions to candidates

Duration: 02 hours
 Number of questions: 06
 Number of questions to be answered: 04
 Mark allocation: 100
 All symbols carry their usual meaning.

1.
 - a. Two solid cylindrical rods AB and BC are welded together at B and loaded as shown in Figure 1(a). If $d_1 = 50$ mm and $d_2 = 30$ mm, find the average normal stress at the midsection of
 - i. rod AB , (30%)
 - ii. rod BC . (20%)
 - b. Link BD is made of brass ($E = 105$ GPa) and has a cross-sectional area of 240 mm². Link CE is made of aluminum ($E = 72$ GPa) and has a cross-sectional area of 300 mm². Links BD and CE support the rigid member ABC as shown in Figure 1(b). Determine the maximum force P that can be applied vertically at point A if the deflection of A is not to exceed 0.35 mm. (50%)

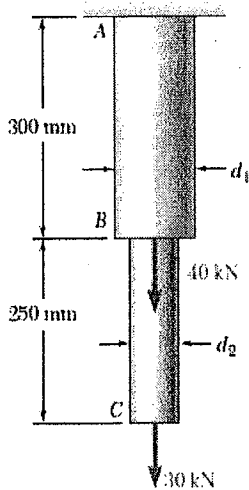


Figure 1(a)

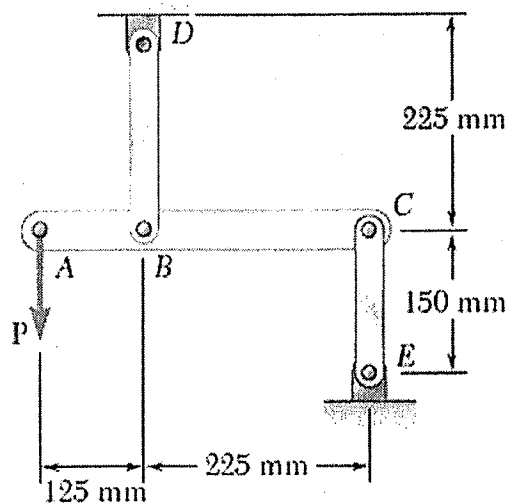


Figure 1(b)

2.
 - a. The torques shown in Figure 2 (a) are exerted on pulleys A and B . If both shafts are solid, determine the maximum shearing stress in
 - i. shaft AB , (30%)
 - ii. shaft BC . (20%)

b. Two solid steel shafts are connected by gears as shown in Figure 2(b). If $G = 80 \text{ GPa}$ for each shaft and that the allowable shearing stress is 55 MPa , determine

- i. the largest torque T_0 that may be applied to the end of shaft AB , (35%)
- ii. the corresponding angle through which end A of shaft AB rotates. (15%)

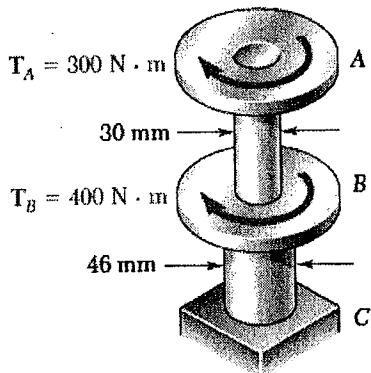


Figure 2 (a)

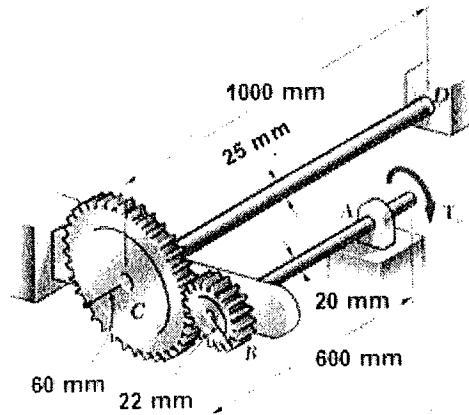


Figure 2(b)

3.

a. Cross-section of a beam is shown in Figure 3(a). Find,

- i. location of the neutral axis for bending in longitudinal direction, (25%)
- ii. second moment of area about the neutral axis. (25%)

b. A W 200 x 31.3 rolled-steel beam is subjected to a couple M of moment 45 kNm . If the Young's modulus, $E = 200 \text{ GPa}$ and the Poisson's ratio, $\nu = 0.29$, determine

- i. the radius of curvature ρ , (25%)
- ii. the radius of curvature ρ' of a transverse cross section. (25%)

Note: An extract of the tables of properties of wide-flange sections is provided

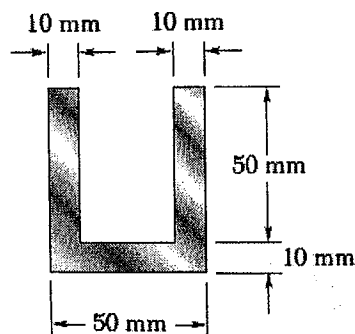


Figure 3(a)

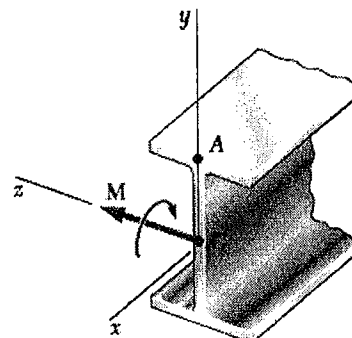


Figure 3(b)

4. Draw the shear and bending-moment diagrams for the rectangular beam and loading shown in Figure 4(a). (60%)

The cross section of the beam is shown in Figure 4(b). Determine the maximum absolute value

- a. of the shear, (15%)
- b. of the bending moment, (15%)
- c. of the normal stress. (10%)

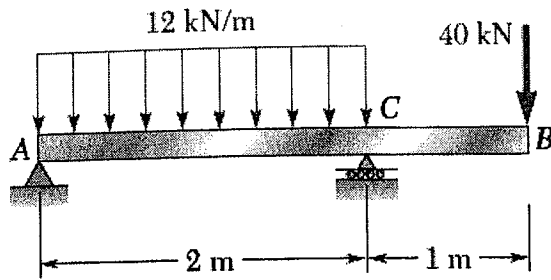


Figure 4(a)

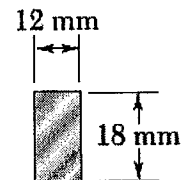


Figure 4(b)

- 5.
- a. For the state of plane stress shown in Figure 5(a), determine the largest value of σ_y for which the maximum in-plane shearing stress is equal to or less than 75 MPa. (50%)
 - b. For the state of stress shown in Figure 5(b), determine the normal and shearing stresses after the element shown has been rotated through
 - i. 25° clockwise, (30%)
 - ii. 10° counterclockwise. (20%)

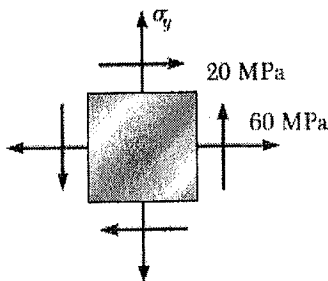


Figure 5(a)

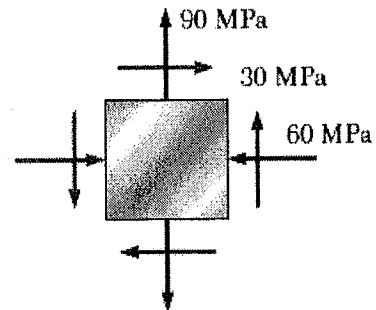


Figure 5(b)

6. Consider the beam and loading shown in Figure 6. If $a = 5.2$ m, $w = 50$ kN/m, and $E = 200$ GPa, determine,

- a. the slope at support A, (50%)
- b. the deflection at the mid-point C. (50%)

Note: An extract of the tables of properties of wide-flange sections is provided



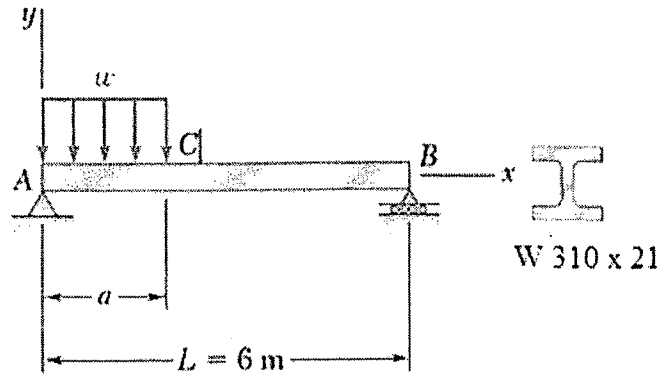


Figure 6